

“Physical conceptions are free creations of the human mind, and are not, however it may seem, uniquely determined by the external world.”

-- Einstein

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Last Time

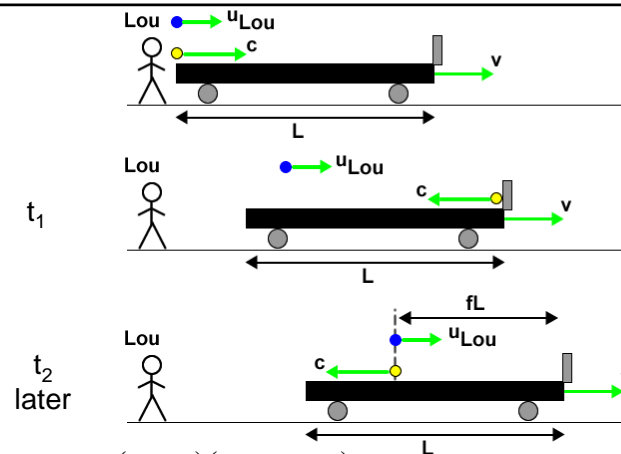
- Relativistic Doppler Effect
- Length Contraction
- Simultaneity
- The Interval
- Spacetime Diagrams
- The Dimensions of Spacetime

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Today

- Addition of Velocities
- Relativistic Momentum
- Relativistic Energy
 - $E = m c^2$

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$$f = \frac{(c + v)(c - u_{Lou})}{(c - v)(c + u_{Lou})}$$

4

Recall (Jan 5, Mar 16): You pursue a sound wave at 99% of the speed of sound relative to the air

You will observe:

- A. A sound wave moving away from you at the speed of sound
- B. A sound wave moving away from you at **about 1% of the speed of sound**
- C. A stationary sound wave
- D. You can not pursue a sound wave at 99% of the speed of sound

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Another Chain of Reasoning

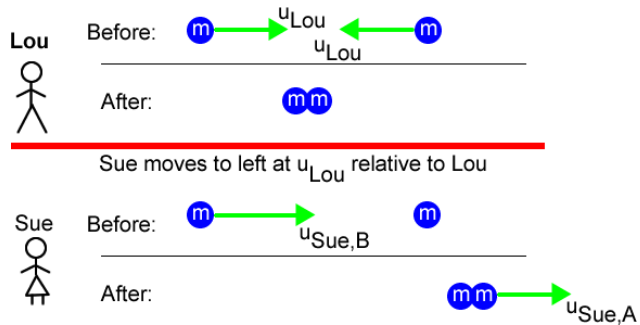
Einstein: the speed of light is the same for all observers

THEREFORE

Velocities do not add according to our common sense

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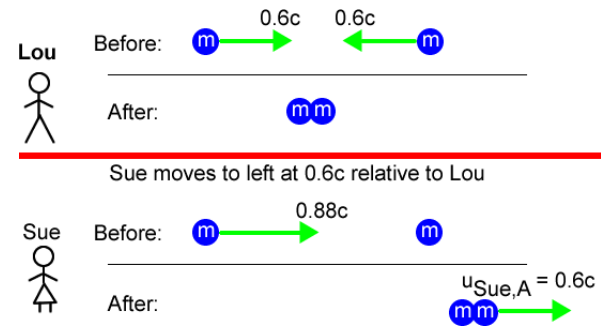
Inelastic Collisions



- $u_{Sue,A}$ is:
- A. $< u_{Lou}$
 - B. $= u_{Lou}$**
 - C. $> u_{Lou}$

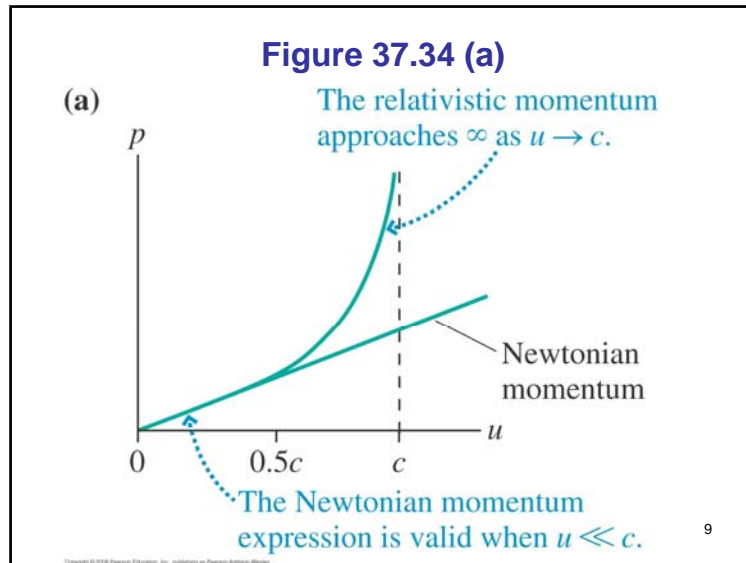
7

Some Numbers



- According to Newtonian Conservation of Momentum, $u_{Sue,A}$ is:
- A. 0
 - B. $0.44c$**
 - C. $0.6c$
 - D. c

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Recall March 23: You pursue a light wave at 99% of the speed of light relative to the source of the light wave

You will observe:

- A. A light wave moving away from you at the speed of light
- B. A light wave moving away from you at about 1% of the speed of light
- C. A stationary light wave
- D. You can not pursue a light wave at 99% of the speed of light

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Einstein (age 16): If you pursue a beam of light at the speed of light relative to the source of the light beam you will see:

- A. The beam of light moving away from you at the speed of light.
- B. A beam of light moving away from you at 1% of the speed of light.
- C. A stationary light wave.
- D. You can not pursue a beam of light at the speed of light.

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Another Chain of Reasoning

Einstein: the speed of light is the same for all observers

THEREFORE

Velocities do not add according to our common sense

THEREFORE

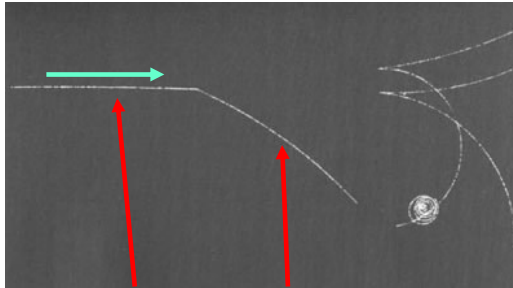
If momentum is conserved it must be

$$\vec{p} = \frac{1}{\sqrt{1 - u^2/c^2}} m\vec{u}$$

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Bubble Chamber

Charged particles leave tracks
Magnetic field into the screen
curves the tracks



$K^- \Rightarrow \pi^- + \pi^0$
 $\pi^0 \Rightarrow 2 \text{ photons}$

Each photon \Rightarrow electron-positron pair ¹³